

# Spatio-Temporal Behavior of Bistable Density Transition in Magnetized Plasma

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Self-excited bistable transition phenomena have been investigated by voltage biasing to an inserted electrode of a radio frequency (rf)-produced, magnetized plasma. Spatio-temporal behaviors of global, density transitions and back ones between two states (flip-flop pattern) have been measured, as to the ion saturation current  $I_{is}$  and floating potential  $V_f$  in the bulk plasma and near the electrode regions. Transition time  $T_{tr}$  between two states was dependent on the bulk region, and it was less than ms and  $\sim$  a few ms for  $I_{is}$  and  $V_f$ , respectively. On the other hand,  $T_{tr}$  was very small for the bias current on the order of  $\sim \mu s$ , and it was also small for  $I_{is}$  and  $V_f$ , which have less than a few tens of  $\mu s$  near the electrode region, where structural changes of plasma potential and density were observed at the transition. These showed the importance of the sheath, electrode region to trigger the transition coming from the two-dimensional particle balance and motion with sheath type instabilities.

**Key words:** *Plasma, Transition, Bistability, Self-excitation, Biasing, Electrode, Electric field, Magnetic field*

## 1. Introduction

Transition and bifurcation phenomena in plasmas have been supplying many various interesting topics in the fields of basic nonlinear physics as well as the fundamental plasma physics including fusion-oriented research. The intrinsically nonlinear characteristics of the plasma exhibit various interesting phenomena<sup>1-19)</sup> such as the self-organized structural formation including hystereses. However, there have been few experiments<sup>5-9)</sup> from a basic viewpoint to study these transitions.

Recently, density transitions in bistable systems were clearly found and reported<sup>20,21)</sup>, by voltage biasing to electrodes inserted into the rf-produced, cylindrical magnetized plasma: density transitions and back ones between two global states, accompanied by potential changes. Control of the staying time and staying probability in one of two states, by

changing the bias voltage, was tried, with also emphasizing hysteresis characteristics in a statistical sense. Although general features of transitions were found in the previous papers<sup>20,21)</sup>, simultaneous spatio-temporal behaviors were not obtained due to the limited channels of the probes and the data acquisition system. Furthermore, the structures near the electrode have not been measured in spite of suggesting its importance of triggering transitions.

Here, we have examined spatio-temporal behaviors of global characteristics of a self-excited bistable system from a viewpoint of the transition times of parameters such as ion saturation current  $I_{is}$ , floating potential  $V_f$ , and bias current  $I_b$ , in order to have a clue of the triggering / governing mechanisms of transitions. In addition to the bulk plasma region, plasma behaviors in the sheath region (near the electrode) were investigated to understand the short transition times such as  $I_b$ , since the potential structure change in this region due to some instabilities, e.g., sheath type instabilities, is considered to initiate the transitions.

Note that these measurements have been possible due to an introduction of the new data acquisition system, multi-channel probe array, and three-dimensional moving system<sup>22)</sup> located near the electrode.

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## 2. Experimental Results

### 2.1 Experimental setup

A typical argon pressure of  $P_0 = 1\text{--}3$  mTorr with the continuous rf power and frequency of  $P_{rf} = 160$  W and  $f_{rf} = 7$  MHz, respectively, were applied to a linear device, 45 cm in outer diameter and 170 cm in axial length, with the magnetic field of 500 G, as shown in Fig.1(a). Here,  $x(z)$  is taken along the radial (axial) direction. We used ten concentric rings as biased electrodes<sup>6,7,9</sup>, and the no. 3 electrode (inner and outer radii are 3.7 and 6 cm, respectively) was used. In addition to the conventional Langmuir probes, we newly installed a 24-channel probe array, as shown in Fig.1(b), and three-dimensional probe moving system<sup>22</sup>. Note that the frequency responses in measuring  $I_{is}$  and  $V_f$  were more than 50 kHz and less than 10 kHz, respectively.

Most of the data were stored in the data logger with a sampling time of 10  $\mu$ s. With the use of the current probe and additional logger, which has the faster sampling time of 50 ns, we could observe the fast change of  $I_b$ . For

controlling the state from I to II or vice versa dynamically, a function generator and an amplifier were also used to change the bias voltage  $V_b$ .

### 2.2 Spatio-temporal behavior and transition time

Figure 2 shows an example of the spatio-temporal behavior as to the global change of radial  $I_{is}$  (proportional to plasma density) and  $V_f$  profiles at  $z = 30$  cm by the 24-channel probe. Transition time  $T_{tr}$  was dependent on radial position, and there were some differences of this time between transitions from state I ( $I_{is}$  was large away from the No.3 electrode axially and in the outer radial region of this electrode) to state II ( $I_{is}$  was small in the above mentioned regions) and from state II to state I. For convenience, this time is defined as the elapsed time to take the values from 20 % to 80 % of the difference between averaged values in state I and state II.

Figure 3 shows  $T_{tr}$  of  $I_{is}$  and  $V_f$  for different axial locations, taken at  $x = 9$  cm (in the outer radial region of the electrode). Both  $I_{is}$  and  $V_f$

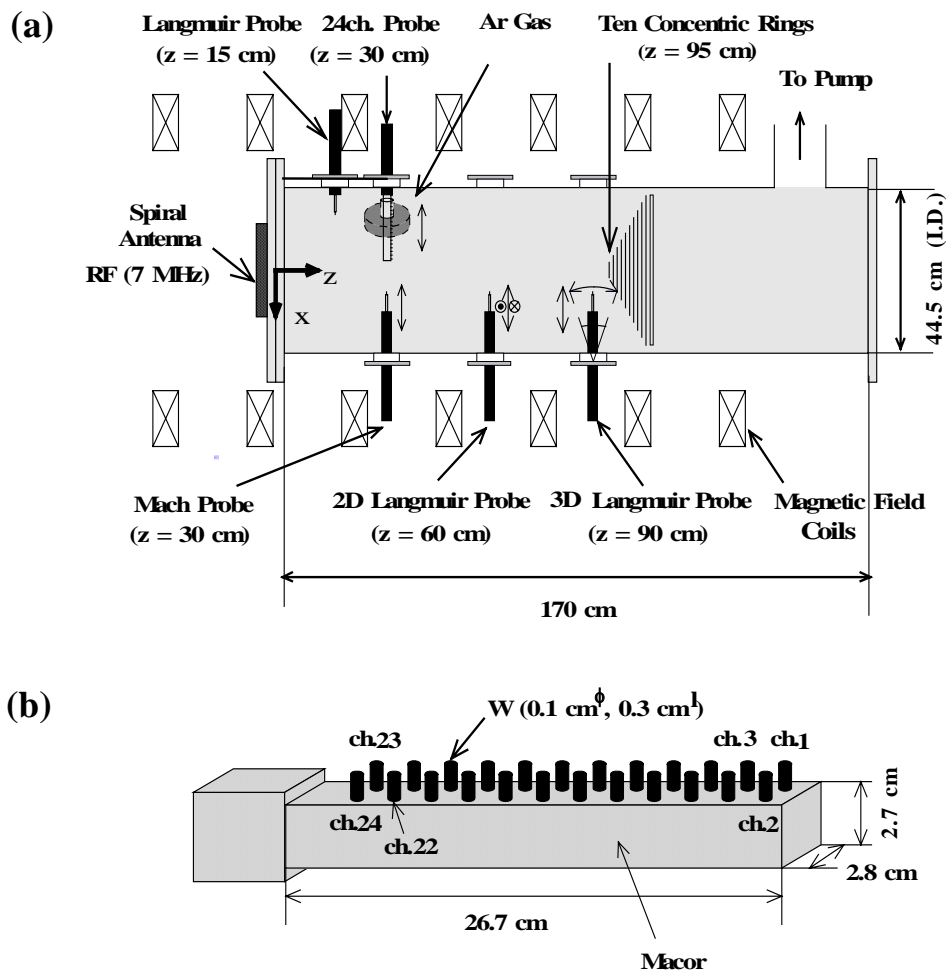
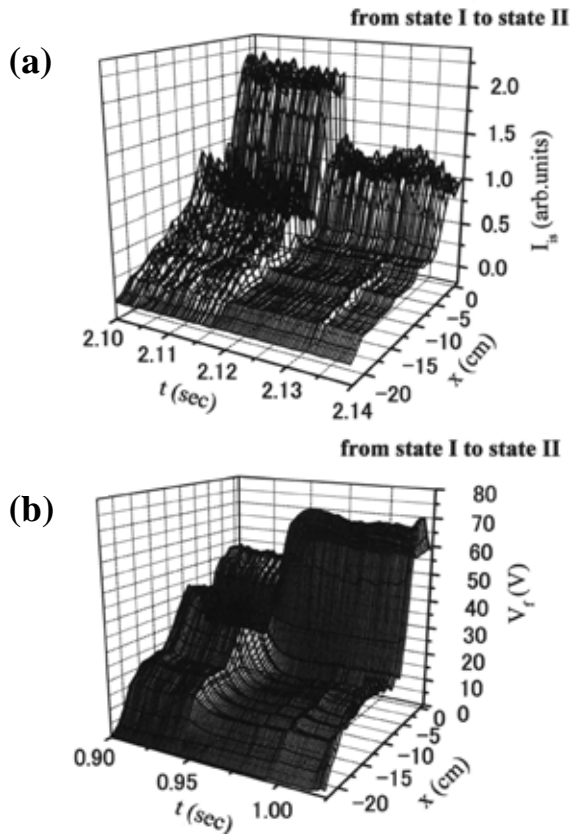


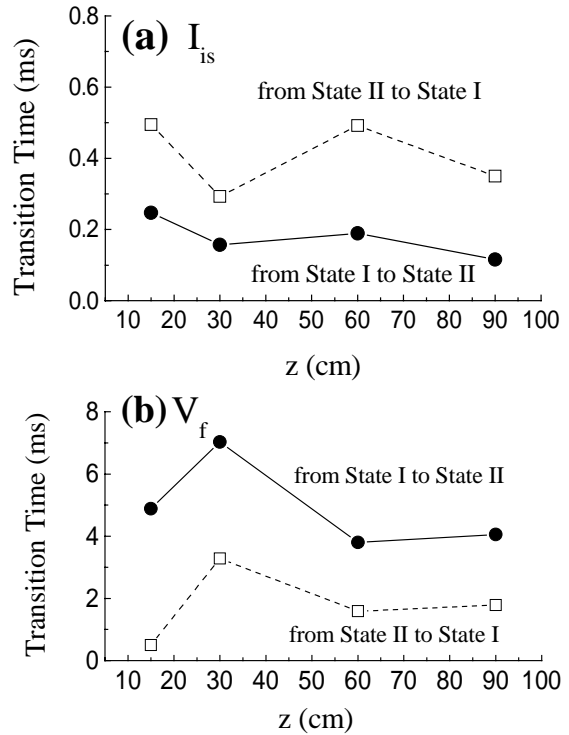
Fig.1 Schematic view of (a) experimental setup and (b) 24-channel probe array.



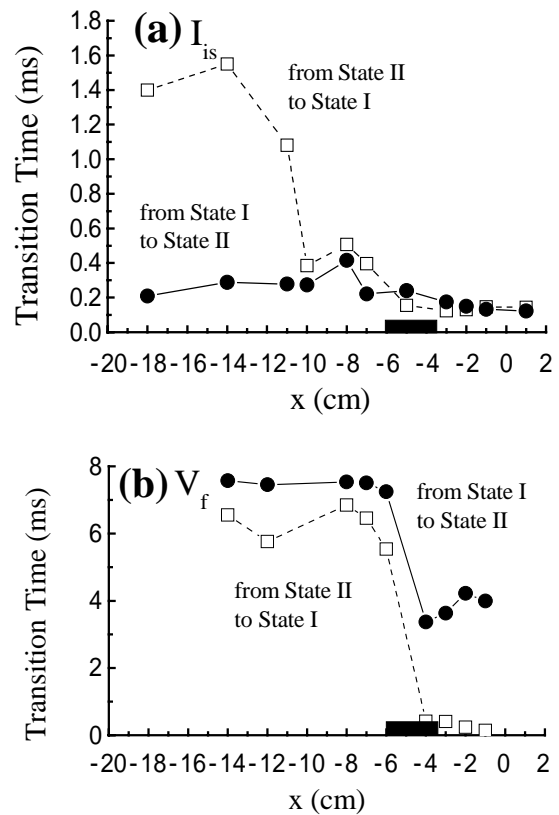
**Fig.2** Spatio-temporal behaviors of (a) ion saturation current  $I_{is}$  and (b) floating potential  $V_f$  (different shots) at  $z = 30$  cm with bias voltage  $V_3 = 160$  V and fill pressure  $P_0 = 2.1$  mTorr, measured by the 24-channel probe.

showed nearly constant  $T_{tr}$  regardless of the axial position. Typical  $T_{tr}$  of  $I_{is}$  was less than 0.5 ms, and  $T_{tr}$  from state I to state II is smaller than that from state II to state I (see also Fig.2). On the other hand, typical  $T_{tr}$  of  $V_f$  was on the order of a few ms, and  $T_{tr}$  from state I to state II is larger than that from state II to state I (see also Fig.2). From this, transitions occur globally at nearly the same rate regardless of the axial position.

Figure 4 shows  $T_{tr}$  of  $I_{is}$  and  $V_f$  for different radial locations, by the 24-channel probe. Different transition times depending on radial locations were found. There was a tendency that  $T_{tr}$ , for both transitions of from state I to state II and from state II to state I, was smaller in the inner radial region of the electrode than that of in the outer region in both cases of  $I_{is}$  and  $V_f$ . This may be related to the smaller plasma volume, which can change the equilibrium in the shorter time if the phenomena between the inner and outer regions are similar. Here, the case of the transition from state I to state II in  $I_{is}$  is an exception:  $T_{tr}$  was nearly constant of  $\sim 0.2$  ms along the radial direction.



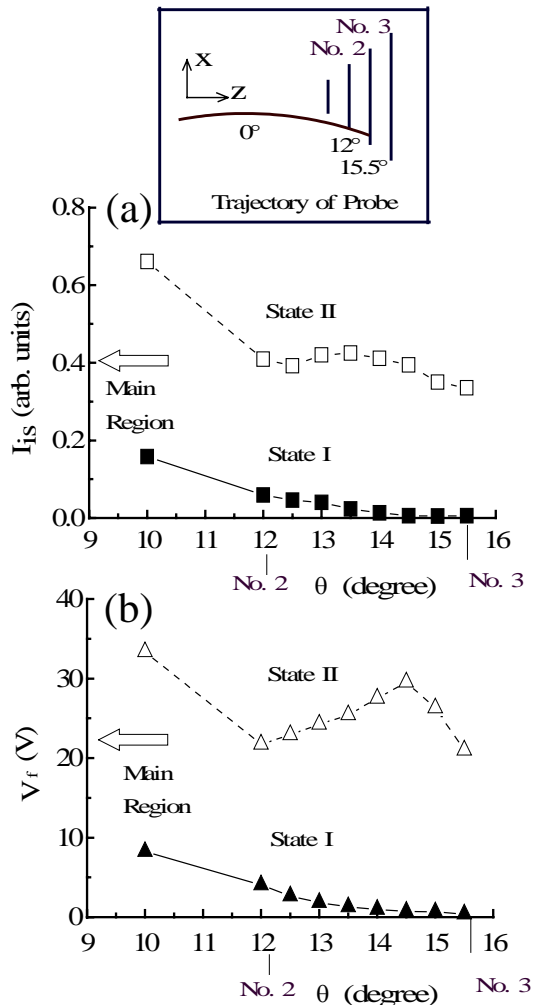
**Fig.3** Transition times of (a)  $I_{is}$  and (b)  $V_f$  on different axial locations. Here, data are taken at  $x = 9$  cm with  $V_3 = 157$  V and  $P_0 = 1.8$  mTorr.



**Fig.4** Transition times of (a)  $I_{is}$  and (b)  $V_f$  as a function of radial position for the same condition as that in Fig. 2. Radial position of no. 3 electrode is denoted as a horizontal closed bar.

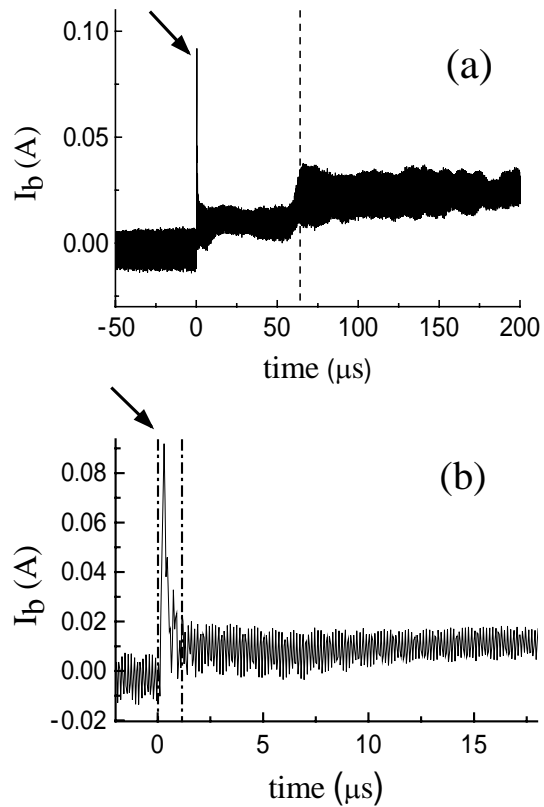
### 2.3 Plasma behavior near electrode

Since the importance of the transitions near the electrode region was suggested, the spatio-temporal behaviors near this region were investigated using the scanned Langmuir probe in three-dimensional direction<sup>22</sup>). Figure 5 shows the spatial profiles of  $I_{is}$  and  $V_f$  in state I and state II. Mostly, this probe was moved along the arc trajectory, as shown in the inset of this figure. The probe position at  $\theta = 12^\circ$  ( $15.5^\circ$ ) corresponds to the outer radial edge of the no.2 electrode (the surface of no.3 electrode). From this,  $I_{is}$  decreased slowly (did not change so much) toward the electrode with  $\theta = 12^\circ$ - $15.5^\circ$  in state I (state II). This  $I_{is}$  was larger in state II than that in state I, which is the opposite behavior in the bulk plasma region, where  $I_{is}$  was larger in state I than that in state II.



**Fig.5** Spatial profiles of (a)  $I_{is}$  and (b)  $V_f$  near the electrode with  $V_3 = 177$  V and  $P_0 = 1.2$  mTorr. Typical values of  $I_{is}$  and  $V_f$  in the main region at the same radial location of no. 3 electrode are shown as arrows, and inset shows a trajectory of the probe.

There is a slight hump of  $I_{is}$  in state II around  $\theta = 13.5^\circ$ , which may correspond the hump of  $V_f$  (virtual anode-like) observed in Fig. 5(b). In state II,  $V_f$  was higher than that in state I by  $> 20$  V. In state I, the value of  $V_f$  was lower than that in the central region (along the  $z$  axis) with  $x = 5$  cm by  $> 15$  V, which shows that the electrons can be trapped easily in the central region. This is consistent with the fact that in the bulk plasma region  $I_{is}$  in state I is larger than that in state II. On the other hand, although the sampling time of  $10 \mu\text{s}$  is not enough,  $I_{is}$  near the electrode region, regardless of  $\theta$ , changed very fast ( $< 10 \mu\text{s}$  transition time) on the same order of the changing time of  $I_b$ , which is much faster than the change of  $I_{is}$  in the bulk region. Here,  $T_r$  of  $V_f$  was also small of less than a few tens of  $\mu\text{s}$  (this time is limited by the measuring system mentioned before). These also show the importance of density transition near the electrode region in addition to the fast  $I_b$  change written below.



**Fig.6** Time evolution of (a)  $I_b$  with  $P_0 = 3.5$  mTorr from state I to state II by the fast rise of  $V_3$  from 110 V to 210 V. Here, Fig. (b) shows time change of  $I_b$  of Fig. (a) in an expanding time scale.

This  $I_b$  change was carefully measured in a controlled manner. As was described, the function generator and the amplifier were used in addition to the fast logger with a sampling

time of 50 ns. Note that this does not mean the self-excited transition, but the forced transition. However, general characteristics such as the  $T_{tr}$  of  $I_{is}$  and  $V_f$  were not changed. Figure 6 shows the time evolution of  $I_b$  by the fast rise of  $V_3$ . Here, the initial (final) voltage  $V_3 = 110$  V (210 V) corresponds to state I only (state II only). At  $t \sim 350$  ns  $I_b$  had a sharp overshoot positive spike, as is shown as an arrow in Fig.6(a), which can be clearly seen in Fig.6(b) in an expanding time scale for a different shot (there was a drift of  $I_b$ : baseline of this current, i.e. zero current, is -10 mA).

The real rise time of  $I_b$  is shorter, which is estimated to be less than several tens of ns, if considering the rise time ( $\sim 300$  ns) of  $V_3$ . Then, the fast decay (e-folding time was  $< 400$  ns) was observed, and after  $t = 1.2 \mu\text{s}$  [the second chained vertical line in Fig. 6(b)],  $I_b$  became steady with some fluctuations. Here, the oscillation period of 143 ns superimposed on this  $I_b$  corresponded to the 7 MHz frequency of the rf power source. Sometimes we could see the fine different structures even in the same state of "state II", which was suggested from the distribution function of  $I_{is}$  in Ref. 21: at  $t = 64 \mu\text{s}$  [a vertical dotted line in Fig. 6(a)], there was the second jump of  $I_b$  and it occupied this new state steadily after that.

### 3. Discussion and Conclusion

The spatio-temporal characteristics of bistable system in a magnetized plasma are discussed, focusing on the triggering/governing mechanisms. This mechanism, which will be described later in detail, can be considered as follows as a promising candidate: a kind of the sheath type instabilities to change the potential structure near the electrode causes the fast change of  $I_b$  by the electron motion along the field on the order of less than several tens of ns. Next, due to the balance of the ambipolarity, ions moves slowly along the field with a time scale of the ion transit time followed by the perpendicular ion motion across the field. Final, another stable equilibrium, i.e., different, global potential and density profiles, in the bulk region is reached on a transport time scale (the ion classical transport across the magnetic field) of a few ms.

Now, detailed characteristics on transition phenomena in the initial phase are discussed. As was mentioned, the behavior near the electrode region is important, since during transitions  $I_b$ ,  $I_{is}$ , and  $V_f$  changed very fast. Furthermore, there were some events with no transitions even though spikes of  $I_b$  were ob-

served. The changing time scale of  $I_b$  was estimated to be less than several tens of ns, which is close to the characteristic time scale of the time-dependent sheath, e.g., Refs. 23 and 24, in the range of ns ( $1/\omega_{pe}$  range). The decay time of  $I_b$  and the time necessary to have the steady condition after the transition for about a few  $\mu\text{s}$  are comparable to the ion transit time through the sheath region. The above behaviors may be related to the sheath and the ion acoustic type instabilities<sup>25)</sup>.

The next phase of transitions is considered. Due to a change of  $I_b$ , keeping the total ambipolarity leads to a change of the perpendicular ion flow due to enhanced diffusion by, e.g., change of some instabilities or turbulent states. Then, the slow change of plasma parameters in the bulk region are expected on a transport time scale. Note that the physical picture of the ion motion across the magnetic field is similar to the one in potential-driven ion cyclotron oscillations in a Q machine<sup>26)</sup>, although the time scale of  $\sim \mu\text{s}$  in our experiments is much shorter than the inverses of the ion cyclotron frequency of  $\sim 50 \mu\text{s}$ . Here, in a Q machine, the cyclotron oscillations were observed when the electrode half radius is larger than the ion Larmor radius. In our case, the transition effect fades out when the number of biased rings was increased, where the radial width of one ring was a few times of the ion Larmor radius.

In order to simulate the observed results, which suggest the sheath type instabilities, two-dimensional particle-in-cell simulations of a magnetized plasma have been carried out<sup>27)</sup>. Preliminary results show that there is an autonomous oscillation: the main oscillation region is limited to the zone in which magnetic field lines are connected with the positively charged electrostatic plate. This is a kind of bifurcation phenomenon and appears with the potential of the plate being less than a critical value. The size of the plate must be finite across the magnetic field, because the electron and ion motions, which are mainly parallel and perpendicular to the magnetic field, respectively, influence the negative sheath facing the plate. The oscillation of the sheath width parallel to the magnetic field is synchronized with that of the amplitude of the potential, and a periodic ion bunching is also observed near the plate. The oscillation period is determined by the transit time of ions, which pass through the sheath region. These behaviors suggest a kind of two-dimensional sheath instability. This should be investigated in detail, and changing gas species may also give additional

information.

For further investigation, it is necessary to have a comparative study between experimental and stimulation results, noting the dynamic change of the two-dimensional sheath structure (local density and potential in a small area) followed by the bulk plasma one. An ion velocity distribution function may be also a key to understand this mechanism as well as the probabilistic transition with hysterese<sup>20,21</sup>.

To summarize, detailed behaviors of the self-excited bistable transition phenomena have been investigated in the bulk as well as electrode regions. Depending on the spatial region, transition time of  $T_{tr}$  was different. Near the electrode, where structural changes of the potential and the density were observed at the transition,  $T_{tr}$  was much shorter than that in the bulk region. These showed the important role of the structural changes to trigger the transitions due to the sheath type instabilities near the electrode. Next process is the ion motion along and across the field, which follows the fast change of  $\bar{b}$ , and final, another stable equilibrium in the bulk plasma is obtained on a transport time scale.

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